# Package ‘dcTensor’ 

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Description Semi-Binary and Semi-Ternary Matrix Decomposition are performed based on Non-negative Matrix Factorization (NMF) and Singular Value Decomposition (SVD). For the de-tails of the methods, see the reference sec-tion of GitHub README.md [https://github.com/rikenbit/dcTensor](https://github.com/rikenbit/dcTensor).
License MIT + file LICENSE
URL https://github.com/rikenbit/dcTensor
VignetteBuilder knitr
NeedsCompilation no
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```
dcTensor-package Discrete Matrix/Tensor Decomposition
```


## Description

Semi-Binary and Semi-Ternary Matrix Decomposition are performed based on Non-negative Matrix Factorization (NMF) and Singular Value Decomposition (SVD). For the details of the methods, see the reference section of GitHub README.md [https://github.com/rikenbit/dcTensor](https://github.com/rikenbit/dcTensor).

## Details

The DESCRIPTION file:

| Package: | dcTensor |
| :--- | :--- |
| Type: | Package |
| Title: | Discrete Matrix/Tensor Decomposition |
| Version: | 1.3 .0 |
| Authors@R: | c(person("Koki", "Tsuyuzaki", role = c("aut", "cre"), email = "k.t.the-answer@hotmail.co.jp")) |
| Depends: | R (>=3.4.0) |
| Imports: | methods, MASS, fields, rTensor, nnTensor |
| Suggests: | knitr, rmarkdown, testthat |
| Description: | Semi-Binary and Semi-Ternary Matrix Decomposition are performed based on Non-negative Matrix Facto |
| License: | MIT + file LICENSE |
| URL: | https://github.com/rikenbit/dcTensor |
| VignetteBuilder: | knitr |
| Author: | Koki Tsuyuzaki [aut, cre] |
| Maintainer: | Koki Tsuyuzaki [k.t.the-answer@hotmail.co.jp](mailto:k.t.the-answer@hotmail.co.jp) |

Index of help topics:

| dNMF | Discretized Non-negative Matrix Factorization <br> Algorithms (dNMF) |
| :--- | :--- |
| dNMTF | Discretized Non-negative Matrix <br> Tri-Factorization Algorithms (dNMTF) |
| dNTD | Discretized Non-negative Tucker Decomposition <br> Algorithms (dNTD) |
| dNTF | Discretized Non-negative CP Decomposition <br> Algorithms (dNTF) |
| dPLS | Discretized Partial Least Squares (dPLS) <br> dSVD (dSVD) <br> dcTensor-package <br> djNMF |
| Discretized Singular Value Decomposition |  |
| dsiNMF | Discrete Matrix/Tensor Decomposition <br> Discretized Joint Non-negative Matrix |
|  | Factorization Algorithms (djNMF) <br> Discretized Simultaneous Non-negative Matrix <br> Factorization Algorithms (dsiNMF) |

toyModel Toy model data for using dNMF, dSVD, dsiNMF, djNMF, dPLS, dNTF, and dNTD

## Author(s)

NA
Maintainer: NA

## References

Z. Zhang, T. Li, C. Ding and X. Zhang, (2007). Binary Matrix Factorization with Applications, Seventh IEEE International Conference on Data Mining (ICDM 2007), 391-400

## See Also

toyModel,dNMF,dSVD

## Examples

ls("package:dcTensor")

```
djNMF
```

Discretized Joint Non-negative Matrix Factorization Algorithms (djNMF)

## Description

This function is the discretized version of nnTensor::jNMF. The input data objects are assumed to be a list containing multiple non-negative matrices ( $\mathrm{X} \_1, \mathrm{X} \_2, \ldots, \mathrm{X} \_\mathrm{K}$ ), and decomposed to multiple matrix products $\left(\left(W+V \_1\right) H_{-} 1^{\prime},\left(W+V \_2\right) H_{-} 2^{\prime}, \ldots\right.$, ( $\mathrm{W}+\mathrm{V} \_\mathrm{K}$ ) $\left.\mathrm{H}_{-} \mathrm{K}^{\prime}\right)$, where W is common across all the data matrices but each $V_{\_} k$ or $H_{-} k(k=1 . . K)$ is specific in each $X_{-} k$. Unlike regular jNMF , in djNMF, W, V_k, and H_k are estimated by adding binary regularization so that the values are 0 or 1 as much as possible. Likewise, W, V_k, and H_k are estimated by adding ternary regularization so that the values are 0,1 , or 2 as much as possible.

## Usage

djNMF (X, M=NULL, pseudocount=.Machine\$double.eps, initW=NULL, initV=NULL, initH=NULL, fixW=FALSE, fixV=FALSE, fixH=FALSE,
Bin_W=1e-10, Bin_V=rep(1e-10, length=length(X)), Bin_H=rep(1e-10, length=length $(X)$ ), Ter_W=1e-10, Ter_V=rep(1e-10, length=length $(X))$, Ter_H=rep(1e-10, length=length $(X))$, L1_W=1e-10, L1_V=rep(1e-10, length=length $(X)$ ), L1_H=rep(1e-10, length=length(X)), L2_W=1e-10, L2_V=rep(1e-10, length=length $(X))$, L2_H=rep(1e-10, length=length $(X)$ ), J = 3, w=NULL, algorithm = c("Frobenius", "KL", "IS", "PLTF"), p=1, thr $=1 \mathrm{e}-10$, num.iter $=100$, viz $=$ FALSE, figdir $=$ NULL, verbose $=$ FALSE)

## Arguments

$\left.\begin{array}{ll}\text { X } & \text { A list containing input matrices }\left(\mathrm{X} \_\mathrm{k},<\mathrm{N} * \mathrm{Mk}>, \mathrm{k}=1 . . \mathrm{K}\right) . \\ \mathrm{M} & \text { A list containing the mask matrices }\left(\mathrm{X} \_\mathrm{k},<\mathrm{N} * \mathrm{Mk}>, \mathrm{k}=1 . . \mathrm{K}\right) \text {. If the input matrix } \\ \text { has missing values, specify the element as } 0 \text { (otherwise 1). }\end{array}\right\}$

| w | Weight vector (Default: NULL) |
| :---: | :---: |
| algorithm | Divergence between X and X_bar. "Frobenius", "KL", and "IS" are available (Default: "KL"). |
| $p$ | The parameter of Probabilistic Latent Tensor Factorization ( $\mathrm{p}=0$ : Frobenius, $\mathrm{p}=1: \mathrm{KL}, \mathrm{p}=2$ : IS) |
| thr | When error change rate is lower than thr, the iteration is terminated (Default: 1E-10). |
| num.iter | The number of interation step (Default: 100). |
| viz | If viz $==$ TRUE, internal reconstructed matrix can be visualized. |
| figdir | the directory for saving the figure, when viz == TRUE. |
| verbose | If verbose $==$ TRUE, Error change rate is generated in console windos. |

## Value

W : A matrix which has N-rows and J -columns ( $\mathrm{J}<\mathrm{N}, \mathrm{Mk}$ ). V : A list which has multiple elements containing N -rows and J -columns ( $\mathrm{J}<\mathrm{N}, \mathrm{Mk}$ ). H : A list which has multiple elements containing Mk-rows and J-columns matrix ( $\mathrm{J}<\mathrm{N}, \mathrm{Mk}$ ). RecError : The reconstruction error between data matrix and reconstructed matrix from W and H . TrainRecError : The reconstruction error calculated by training set (observed values specified by M). TestRecError : The reconstruction error calculated by test set (missing values specified by $M$ ). RelChange : The relative change of the error.

## Author(s)

Koki Tsuyuzaki

## References

Liviu Badea, (2008) Extracting Gene Expression Profiles Common to Colon and Pancreatic Adenocarcinoma using Simultaneous nonnegative matrix factorization. Pacific Symposium on Biocomputing 13:279-290
Shihua Zhang, et al. (2012) Discovery of multi-dimensional modules by integrative analysis of cancer genomic data. Nucleic Acids Research 40(19), 9379-9391

Zi Yang, et al. (2016) A non-negative matrix factorization method for detecting modules in heterogeneous omics multi-modal data, Bioinformatics 32(1), 1-8
Y. Kenan Yilmaz et al., (2010) Probabilistic Latent Tensor Factorization, International Conference on Latent Variable Analysis and Signal Separation 346-353
N. Fujita et al., (2018) Biomarker discovery by integrated joint non-negative matrix factorization and pathway signature analyses, Scientific Report

## Examples

```
matdata <- toyModel(model = "dsiNMF_Hard")
out <- djNMF(matdata, J=2, num.iter=2)
```


## Description

This function is the discretized version of nnTensor::NMF. The input data $X$ is assumed to be a nonnegative matrix and decomposed to a matrix product $U^{\prime}$ '. Unlike regular NMF, in dNMF, U and V are estimated by adding binary regularization so that the values are 0 or 1 as much as possible. Likewise, U and V are estimated by adding ternary regularization so that the values are 0,1 , or 2 as much as possible.

## Usage

dNMF (X, M=NULL, pseudocount=.Machine\$double.eps, initU=NULL, initV=NULL, fixU=FALSE, fixV=FALSE, Bin_U=1e-10, Bin_V=1e-10, Ter_U=1e-10, Ter_V=1e-10, L1_U=1e-10, L1_V=1e-10, L2_U=1e-10, L2_V=1e-10, J = 3, algorithm = c("Frobenius", "KL", "IS", "Beta"), Beta = 2, thr $=1 \mathrm{e}-10$, num.iter $=100$, viz = FALSE, figdir = NULL, verbose = FALSE)

## Arguments

X
M The mask matrix which has N-rows and M-columns. If the input matrix has missing values, specify the element as 0 (otherwise 1 ).
pseudocount The pseudo count to avoid zero division, when the element is zero (Default: Machine Epsilon).
initU The initial values of factor matrix $U$, which has N-rows and J-columns (Default: NULL).
initV The initial values of factor matrix V, which has M-rows and J-columns (Default: NULL).
fixU Whether the factor matrix $U$ is updated in each iteration step (Default: FALSE).
fixV Whether the factor matrix V is updated in each iteration step (Default: FALSE).
Bin_U Paramter for binary $(0,1)$ regularitation (Default: 1e-10).
Bin_V Paramter for binary $(0,1)$ regularitation (Default: 1e-10).
Ter_U Paramter for terary $(0,1,2)$ regularitation (Default: 1e-10).
Ter_V Paramter for terary $(0,1,2)$ regularitation (Default: 1e-10).
L1_U Paramter for L1 regularitation (Default: 1e-10). This also works as small positive constant to prevent division by zero, so should be set as 0 .
L1_V Paramter for L1 regularitation (Default: 1e-10). This also works as small positive constant to prevent division by zero, so should be set as 0 .
L2_U Paramter for L2 regularitation (Default: 1e-10).

| L2_V | Paramter for L2 regularitation (Default: 1e-10). |
| :---: | :---: |
| J | The number of low-dimension ( $\mathrm{J}<\{\mathrm{N}, \mathrm{M}\}$, Default: 3) |
| algorithm | dNMF algorithms. "Frobenius", "KL", "IS", and "Beta" are available (Default: "Frobenius"). |
| Beta | The parameter of Beta-divergence. |
| thr | When error change rate is lower than thr, the iteration is terminated (Default: 1E-10). |
| num.iter | The number of interation step (Default: 100). |
| viz | If viz $==$ TRUE, internal reconstructed matrix can be visualized. |
| figdir | The directory for saving the figure, when viz == TRUE. |
| verbose | If verbose $==$ TRUE, Error change rate is generated in console window. |

## Value

U : A matrix which has N-rows and J-columns ( $\mathrm{J}<\{\mathrm{N}, \mathrm{M}\}$ ). V : A matrix which has M-rows and J-columns ( $\mathrm{J}<\{\mathrm{N}, \mathrm{M}\}$ ). RecError : The reconstruction error between data tensor and reconstructed tensor from U and V . TrainRecError : The reconstruction error calculated by training set (observed values specified by M). TestRecError : The reconstruction error calculated by test set (missing values specified by M). RelChange : The relative change of the error.

## Author(s)

Koki Tsuyuzaki

## References

Z. Zhang, T. Li, C. Ding and X. Zhang, (2007). Binary Matrix Factorization with Applications, Seventh IEEE International Conference on Data Mining (ICDM 2007), 391-400

## Examples

```
# Test data
matdata <- toyModel(model = "dNMF")
# Simple usage
out <- dNMF(matdata, J=5)
```

| dNMTF | Discretized Non-negative Matrix Tri-Factorization Algorithms $(d N$ - <br> $M T F)$ |
| :--- | :--- |

## Description

This function is the discretized version of nnTensor::NMTF. The input data is assumed to be nonnegative matrix. dNMTF decompose the matrix to three low-dimensional factor matices.

## Usage

```
dNMTF(X, M=NULL, pseudocount=.Machine\$double.eps,
```

        initU=NULL, initS=NULL, initV=NULL,
        fixU=FALSE, fixS=FALSE, fixV=FALSE,
        \(B i n \_U=1 e-10, B i n_{-} S=1 e-10\), \(B i n \_V=1 e-10\),
        Ter_U=1e-10, Ter_S=1e-10, Ter_V=1e-10,
        L1_U=1e-10, L1_S=1e-10, L1_V=1e-10,
        L2_U=1e-10, L2_S=1e-10, L2_V=1e-10,
        rank \(=c(3,4)\),
        algorithm = c("Frobenius", "KL", "IS", "Beta"),
        Beta \(=2\), root \(=\) FALSE, thr \(=1 \mathrm{e}-10\), num.iter \(=100\),
        viz = FALSE, figdir = NULL, verbose = FALSE)
    
## Arguments

X
M The mask matrix which has N-rows and M-columns. If the input matrix has missing values, specify the elements as 0 (otherwise 1 ).
pseudocount The pseudo count to avoid zero division, when the element is zero (Default: Machine Epsilon).
initU The initial values of factor matrix U, which has N-rows and J1-columns (Default: NULL).
inits The initial values of factor matrix S, which has J1-rows and J2-columns (Default: NULL).
initV The initial values of factor matrix V, which has M-rows and J2-columns (Default: NULL).
fixU Whether the factor matrix $U$ is updated in each iteration step (Default: FALSE).
fixs Whether the factor matrix $S$ is updated in each iteration step (Default: FALSE).
fixV Whether the factor matrix $V$ is updated in each iteration step (Default: FALSE).
Bin_U Paramter for binary $(0,1)$ regularitation (Default: 1e-10).
Bin_S Paramter for binary $(0,1)$ regularitation (Default: 1e-10).
Bin_V Paramter for binary $(0,1)$ regularitation (Default: 1e-10).
Ter_U Paramter for terary $(0,1,2)$ regularitation (Default: 1e-10).
Ter_S Paramter for terary $(0,1,2)$ regularitation (Default: 1e-10).
Ter_V Paramter for terary $(0,1,2)$ regularitation (Default: 1e-10).
L1_U Paramter for L1 regularitation (Default: 1e-10).
L1_S Paramter for L1 regularitation (Default: 1e-10).
L1_V Paramter for L1 regularitation (Default: 1e-10).
L2_U Paramter for L2 regularitation (Default: 1e-10).
L2_S Paramter for L2 regularitation (Default: 1e-10).
L2_V Paramter for L2 regularitation (Default: 1e-10).
rank The number of low-dimension (J1 ( $<\mathrm{N}$ ) and J2 ( $<\mathrm{M}$ )) (Default: c $(3,4)$ ).

| algorithm | dNMTF algorithms. "Frobenius", "KL", "IS", and "Beta" are available (Default: <br> "Frobenius"). |
| :--- | :--- |
| Beta | The parameter of Beta-divergence (Default: 2, which means "Frobenius"). |
| root | Whether square root is calculed in each iteration (Default: FALSE). |
| thr | When error change rate is lower than thr, the iteration is terminated (Default: |
|  | 1E-10). |
| num.iter | The number of interation step (Default: 100). |
| viz | If viz == TRUE, internal reconstructed matrix can be visualized. |
| figdir | The directory for saving the figure, when viz == TRUE. |
| verbose | If verbose == TRUE, Error change rate is generated in console window. |

## Value

$\mathrm{U}:$ A matrix which has N-rows and J1-columns $(\mathrm{J} 1<\mathrm{N})$. S : A matrix which has J1-rows and J2-columns. V : A matrix which has M-rows and J2-columns (J2 < M). rank : The number of lowdimension $(\mathrm{J} 1(<\mathrm{N})$ and $\mathrm{J} 2(<\mathrm{M})$ ). RecError : The reconstruction error between data tensor and reconstructed tensor from U and $V$. TrainRecError : The reconstruction error calculated by training set (observed values specified by M). TestRecError : The reconstruction error calculated by test set (missing values specified by M). RelChange : The relative change of the error. algorithm: algorithm specified.

## Author(s)

## Koki Tsuyuzaki

## References

Fast Optimization of Non-Negative Matrix Tri-Factorization: Supporting Information, Andrej Copar, et. al., PLOS ONE, 14(6), e0217994, 2019
Co-clustering by Block Value Decomposition, Bo Long et al., SIGKDD'05, 2005
Orthogonal Nonnegative Matrix Tri-Factorizations for Clustering, Chris Ding et. al., 12th ACM SIGKDD, 2006

## Examples

```
    if(interactive()){
        # Test data
        matdata <- toyModel(model = "dNMF")
        # Simple usage
        out <- dNMTF(matdata, rank=c(4,4))
    }
```


## Description

This function is the discretized version of nnTensor::NTD. The input data $X$ is assumed to be a nonnegative tensor and decomposed to a product of a dense core tensor (S) and low-dimensional factor matrices ( $A \_k, k=1 . . K$ ). Unlike regular NTD, in dNTD, each A_k is estimated by adding binary regularization so that the values are 0 or 1 as much as possible. Likewise, each A_k are estimated by adding ternary regularization so that the values are 0,1 , or 2 as much as possible.

```
Usage
    dNTD(X, M=NULL, pseudocount=.Machine$double.eps,
        initS=NULL, initA=NULL, fixS=FALSE, fixA=FALSE,
        Bin_A=rep(1e-10, length=length(dim(X))),
        Ter_A=rep(1e-10, length=length(dim(X))),
        L1_A=rep(1e-10, length=length(dim(X))),
        L2_A=rep(1e-10, length=length(dim(X))),
        rank = rep(3, length=length(dim(X))),
        modes = seq_along(dim(X)),
        algorithm = c("Frobenius", "KL", "IS", "Beta"),
        init = c("dNMF", "Random"),
        Beta = 2, thr = 1e-10, num.iter = 100,
        viz = FALSE,
        figdir = NULL, verbose = FALSE)
```


## Arguments

$X \quad$ K-order input tensor which has I_1, I_2, ..., and I_K dimensions.
M K-order mask tensor which has I_1, I_2, ... and I_K dimensions. If the mask tensor has missing values, specify the element as 0 (otherwise 1 ).
pseudocount The pseudo count to avoid zero division, when the element is zero (Default: Machine Epsilon).
inits The initial values of core tensor which has I_1, I_2, ..., and I_K dimensions (Default: NULL).
initA A list containing the initial values of K factor matrices (A_k, <Ik*Jk>, k=1..K, Default: NULL).
fixS Whether the core tensor $S$ is updated in each iteration step (Default: FALSE).
fixA Whether the factor matrices Ak are updated in each iteration step (Default: FALSE).
Bin_A A K-length vector containing the paramters for binary $(0,1)$ regularitation (Default: $\operatorname{rep}(1 \mathrm{e}-10$, length $=$ length $(\operatorname{dim}(\mathrm{X})))$ ).
Ter_A A K-length vector containing the paramters for terary $(0,1,2)$ regularitation (Default: rep(1e-10, length $=$ length $(\operatorname{dim}(X))))$.

| L1_A | A K-length vector containing the paramters for L 1 regularitation (Default: rep(1e10 , length $=$ length $(\operatorname{dim}(X))))$. This also works as small positive constant to prevent division by zero, so should be set as 0 . |
| :---: | :---: |
| L2_A | A K-length vector containing the paramters for L 2 regularitation (Default: rep(1e10 , length $=$ length $(\operatorname{dim}(X)))$ ). |
| rank | The number of low-dimension in each mode (Default: 3 for each mode). |
| modes | The vector of the modes on which to perform the decomposition (Default: 1:K <all modes>). |
| algorithm | dNTD algorithms. "Frobenius", "KL", "IS", and "Beta" are available (Default: "Frobenius"). |
| init | The initialization algorithms. "NMF", "ALS", and "Random" are available (Default: "NMF"). |
| Beta | The parameter of Beta-divergence. |
| thr | When error change rate is lower than thr1, the iteration is terminated (Default: 1E-10). |
| num.iter | The number of interation step (Default: 100). |
| viz | If viz == TRUE, internal reconstructed tensor can be visualized. |
| figdir | the directory for saving the figure, when viz == TRUE (Default: NULL). |
| verbose | If verbose $==$ TRUE, Error change rate is generated in console windos. |

## Value

S : K-order tensor object, which is defined as S 4 class of rTensor package. A : A list containing K factor matrices. RecError : The reconstruction error between data tensor and reconstructed tensor from $S$ and A. TrainRecError : The reconstruction error calculated by training set (observed values specified by M). TestRecError : The reconstruction error calculated by test set (missing values specified by M). RelChange : The relative change of the error.

## Author(s)

Koki Tsuyuzaki

## References

Yong-Deok Kim et. al., (2007). Nonnegative Tucker Decomposition. IEEE Conference on Computer Vision and Pattern Recognition
Yong-Deok Kim et. al., (2008). Nonneegative Tucker Decomposition With Alpha-Divergence. IEEE International Conference on Acoustics, Speech and Signal Processing
Anh Huy Phan, (2008). Fast and efficient algorithms for nonnegative Tucker decomposition. Advances in Neural Networks - ISNN2008
Anh Hyu Phan et. al. (2011). Extended HALS algorithm for nonnegative Tucker decomposition and its applications for multiway analysis and classification. Neurocomputing

## See Also

plotTensor3D

## Examples

```
tensordata <- toyModel(model = "dNTD")
out <- dNTD(tensordata, rank=c(2,2,2), algorithm="Frobenius",
    init="Random", num.iter=2)
```

```
dNTF
```


## Description

This function is the discretized version of nnTensor::NTF. The input data $X$ is assumed to be a nonnegative tensor and decomposed to a product of a diagonal core tensor (S) and low-dimensional factor matrices (A_k, $k=1$.. K). Unlike regular NTF, in dNTF, each A_k is estimated by adding binary regularization so that the values are 0 or 1 as much as possible. Likewise, each A_k are estimated by adding ternary regularization so that the values are 0,1 , or 2 as much as possible.

## Usage

dNTF (X, M=NULL, pseudocount=.Machine\$double.eps, initA=NULL, fixA=FALSE, Bin_A=rep(1e-10, length=length(dim(X))), Ter_A=rep(1e-10, length=length $(\operatorname{dim}(X)))$, L1_A=rep(1e-10, length=length(dim(X))), L2_A=rep(1e-10, length=length( $\operatorname{dim}(X)))$, rank $=3$, algorithm = c("Frobenius", "KL", "IS", "Beta"), init = c("dNMF", "Random"), Beta $=2$, thr $=1 \mathrm{e}-10$, num.iter $=100$, viz $=$ FALSE, figdir $=$ NULL, verbose = FALSE)

## Arguments

| X | K-order input tensor which has I_1, I_2, ..., and I_K dimensions. |
| :---: | :---: |
| M | K-order mask tensor which has I_1, I_2, ..., and I_K dimensions. If the mask tensor has missing values, specify the element as 0 (otherwise 1 ). |
| pseudocount | The pseudo count to avoid zero division, when the element is zero (Default: Machine Epsilon). |
| initA | A list containing the initial values of K factor matrices (A_k, $\langle\mathrm{Ik} * \mathrm{Jk}\rangle, \mathrm{k}=1 . . \mathrm{K}$, Default: NULL). |
| fixA | Whether the factor matrices Ak are updated in each iteration step (Default: FALSE). |
| Bin_A | A K-length vector containing the paramters for binary $(0,1)$ regularitation (Default: $\operatorname{rep}(1 \mathrm{e}-10$, length=length $(\operatorname{dim}(\mathrm{X})))$ ). |
| Ter_A | A K-length vector containing the paramters for terary $(0,1,2)$ regularitation (Default: $\operatorname{rep}(1 \mathrm{e}-10$, length $=$ length $(\operatorname{dim}(\mathrm{X})))$ ). |


| L1_A | A K-length vector containing the paramters for L 1 regularitation (Default: rep(1e 10 , length=length $(\operatorname{dim}(\mathrm{X})))$ ). This also works as small positive constant to prevent division by zero, so should be set as 0 . |
| :---: | :---: |
| L2_A | A K-length vector containing the paramters for L 2 regularitation (Default: rep(1e10 , length $=$ length $(\operatorname{dim}(X)))$ ). |
| rank | The number of low-dimension in each mode (Default: 3 ). |
| algorithm | dNTF algorithms. "Frobenius", "KL", "IS", and "Beta" are available (Default: "Frobenius"). |
| init | The initialization algorithms. "dNMF", and "Random" are available (Default: "dNMF"). |
| Beta | The parameter of Beta-divergence. |
| thr | When error change rate is lower than thr1, the iteration is terminated (Default: 1E-10). |
| num.iter | The number of interation step (Default: 100). |
| viz | If viz $==$ TRUE, internal reconstructed tensor can be visualized. |
| figdir | the directory for saving the figure, when viz == TRUE (Default: NULL). |
| verbose | If verbose $==$ TRUE, Error change rate is generated in console windos. |

## Value

S : K-order tensor object, which is defined as S4 class of rTensor package. A : A list containing K factor matrices. RecError : The reconstruction error between data tensor and reconstructed tensor from $S$ and $A$. TrainRecError : The reconstruction error calculated by training set (observed values specified by M). TestRecError : The reconstruction error calculated by test set (missing values specified by M). RelChange : The relative change of the error.

## Author(s)

Koki Tsuyuzaki

## References

Andrzej CICHOCKI et. al., (2007). Non-negative Tensor Factorization using Alpha and Beta Divergence. IEEE ICASSP 2007

Anh Huy PHAN et. al., (2008). Multi-way Nonnegative Tensor Factorization Using Fast Hierarchical Alternating Least Squares Algorithm (HALS). NOLTA2008

Andrzej CICHOCKI et. al., (2008). Fast Local Algorithms for Large Scale Nonnegative Matrix and Tensor Factorizations. IEICE Transactions on Fundamentals of Electronics, Communications and Computer Sciences

## See Also

```
plotTensor3D
```


## Examples

tensordata <- toyModel(model = "dNTF")
out <- dNTF(tensordata, rank=3, num.iter=2)
dPLS
Discretized Partial Least Squares (dPLS)

## Description

This function is the discretized version of PLS. The input data objects are assumed to be a list containing multiple matrices ( $\mathrm{X} \_1, \mathrm{X} \_2, \ldots, \mathrm{X} \_\mathrm{K}$ ), and decomposed to multiple matrix products ( $U_{-} 1 V_{-} 1^{\prime}, U_{\_} 2 V_{-} 2^{\prime}, \ldots, U_{-} K V_{-} K^{\prime}$ ), where each $U_{\_} k$ and $V_{-} k(k=1 . . K)$ is specific in each $X_{-} k$. Unlike regular PLS, in dPLS, $U \_k$ and $V \_k$ are estimated by adding ternary regularization so that the values are $-1,0$, or 1 as much as possible.

## Usage

dPLS(X, M=NULL, pseudocount=.Machine\$double.eps, initV=NULL, fixV=FALSE, Ter_V=1e-10, L1_V=1e-10, L2_V=1e-10, eta=1e+10, J = 3, thr $=1 \mathrm{e}-10$, num.iter $=100$, viz $=$ FALSE, figdir $=$ NULL, verbose $=$ FALSE)

## Arguments

$\mathrm{X} \quad$ The input matrix which has N -rows and M -columns.
M The mask matrix which has N-rows and M-columns. If the input matrix has missing values, specify the element as 0 (otherwise 1 ).
pseudocount The pseudo count to avoid zero division, when the element is zero (Default: Machine Epsilon).
initV The initial values of factor matrix V, which has M-rows and J-columns (Default: NULL).
fixV Whether the factor matrix $V$ is updated in each iteration step (Default: FALSE).
Ter_V Paramter for terary ( $-1,0,1$ ) regularitation (Default: 1e-10).
L1_V Paramter for L1 regularitation (Default: 1e-10). This also works as small positive constant to prevent division by zero, so should be set as 0 .
L2_V Paramter for L2 regularitation (Default: 1e-10).
eta Stepsize of gradient descent algorithm (Default: 1e+10).
J The number of low-dimension (J < $\{\mathrm{N}, \mathrm{M}\}$, Default: 3)
thr When error change rate is lower than thr, the iteration is terminated (Default: 1E-10).
num.iter The number of interation step (Default: 100).
viz If viz $==$ TRUE, internal reconstructed matrix can be visualized.
figdir The directory for saving the figure, when viz == TRUE.
verbose If verbose == TRUE, Error change rate is generated in console window.

## Value

$\mathrm{U}:$ A matrix which has N -rows and J-columns $(\mathrm{J}<\{\mathrm{N}, \mathrm{M}\})$. V : A matrix which has M-rows and J-columns ( $\mathbf{J}<\{\mathrm{N}, \mathrm{M}\}$ ). RecError : The reconstruction error between data tensor and reconstructed tensor from U and V. TrainRecError : The reconstruction error calculated by training set (observed values specified by M). TestRecError : The reconstruction error calculated by test set (missing values specified by M). RelChange : The relative change of the error.

## Author(s)

## Koki Tsuyuzaki

## Examples

```
# Test data
matdata <- toyModel(model = "dPLS_Easy")
# Simple usage
out <- dPLS(matdata, J=2, num.iter=2)
```

dsiNMF Discretized Simultaneous Non-negative Matrix Factorization Algo- rithms (dsiNMF)

## Description

This function is the discretized version of nnTensor::siNMF. The input data objects are assumed to be a list containing multiple non-negative matrices ( $\mathrm{X} \_1, \mathrm{X} \_2, \ldots, \mathrm{X} \_\mathrm{K}$ ), and decomposed to multiple matrix products ( W H_1', W H_2', ..., W H_K'), where W is common across all the data matrices but each $H_{-} k(k=1 . . \mathrm{K})$ is specific in each $X \_k$. Unlike regular siNMF, in dsiNMF, W and $\mathrm{H} \_\mathrm{k}$ are estimated by adding binary regularization so that the values are 0 or 1 as much as possible. Likewise, W and $\mathrm{H}_{\mathrm{l}} \mathrm{k}$ are estimated by adding ternary regularization so that the values are 0 , 1 , or 2 as much as possible.

## Usage

dsiNMF (X, M=NULL, pseudocount=.Machine\$double.eps, initW=NULL, initH=NULL, fixW=FALSE, fixH=FALSE, Bin_W=1e-10, Bin_H=rep(1e-10, length=length $(X)$ ), Ter_W=1e-10, Ter_H=rep(1e-10, length=length $(X)$ ), L1_W=1e-10, L1_H=rep(1e-10, length=length $(X)$ ), L2_W=1e-10, L2_H=rep(1e-10, length=length $(X)$ ), J = 3, w=NULL, algorithm = c("Frobenius", "KL", "IS", "PLTF"), p=1, thr $=1 \mathrm{e}-10$, num.iter $=100$, viz $=$ FALSE, figdir $=$ NULL, verbose $=$ FALSE)

## Arguments

X
M
pseudocount The pseudo count to avoid zero division, when the element is zero (Default: Machine Epsilon).
initW The initial values of factor matrix W, which has N-rows and J-columns (Default: NULL).
inith A list containing the initial values of multiple factor matrices (H_k, <Mk*J>, $\mathrm{k}=1$..K, Default: NULL).
fixW Whether the factor matrix W is updated in each iteration step (Default: FALSE).
fixH Whether the factor matrices Hk are updated in each iteration step (Default: FALSE).
Bin_W Paramter for binary $(0,1)$ regularitation (Default: 1e-10).
Bin_H A K-length vector containing the paramters for binary $(0,1)$ regularitation (Default: $\operatorname{rep}(1 \mathrm{e}-10$, length $=$ length $(\operatorname{dim}(\mathrm{X})))$ ). Paramter for terary $(0,1,2)$ regularitation (Default: 1e-10).
A K-length vector containing the paramters for terary $(0,1,2)$ regularitation (Default: $\operatorname{rep}(1 \mathrm{e}-10$, length $=$ length $(\operatorname{dim}(X))))$.
L1_W Paramter for L1 regularitation (Default: 1e-10). This also works as small positive constant to prevent division by zero, so should be set as 0 .
L1_H A K-length vector containing the paramters for L1 regularitation (Default: rep(1e10 , length $=$ length $(\operatorname{dim}(\mathrm{X}))))$. This also works as small positive constant to prevent division by zero, so should be set as 0 .
L2_W Paramter for L2 regularitation (Default: 1e-10).
L2_H A K-length vector containing the paramters for L 2 regularitation (Default: rep(1e10, length=length $(\operatorname{dim}(X))))$.
Number of low-dimension ( $\mathrm{J}<\mathrm{N}, \mathrm{Mk}$ ).
w Weight vector (Default: NULL)
algorithm Divergence between X and X_bar. "Frobenius", "KL", and "IS" are available (Default: "KL").
The parameter of Probabilistic Latent Tensor Factorization ( $\mathrm{p}=0$ : Frobenius, $\mathrm{p}=1$ : KL, $\mathrm{p}=2$ : IS)
thr When error change rate is lower than thr, the iteration is terminated (Default: 1E-10).
The number of interation step (Default: 100).
num.iter
If $v i z==$ TRUE, internal reconstructed matrix can be visualized.
figdir
verbose
A list containing the input matrices ( $\mathrm{X} \_\mathrm{k},<\mathrm{N}^{*} \mathrm{Mk}>, \mathrm{k}=1 . . \mathrm{K}$ ).
A list containing the mask matrices ( $\mathrm{X} \_\mathrm{k},<\mathrm{N} * \mathrm{Mk}>, \mathrm{k}=1$..K). If the input matrix has missing values, specify the element as 0 (otherwise 1 ).
the directory for saving the figure, when viz $==$ TRUE.
If verbose $==$ TRUE, Error change rate is generated in console windos.

## Value

W : A matrix which has N -rows and J-columns ( $\mathrm{J}<\mathrm{N}, \mathrm{Mk}$ ). H : A list which has multiple elements containing Mk-rows and J-columns matrix ( $\mathrm{J}<\mathrm{N}, \mathrm{Mk}$ ). RecError : The reconstruction error between data matrix and reconstructed matrix from W and H . TrainRecError : The reconstruction error calculated by training set (observed values specified by M). TestRecError : The reconstruction error calculated by test set (missing values specified by M). RelChange : The relative change of the error.

## Author(s)

Koki Tsuyuzaki

## References

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## Examples

```
matdata <- toyModel(model = "dsiNMF_Easy")
```

out <- dsiNMF(matdata, J=2, num.iter=2)

## Description

This function is the discretized version of SVD. The input data X is decomposed to a matrix product U V'. Unlike regular SVD, in dSVD, U and V are estimated by adding binary regularization so that the values are 0 or 1 as much as possible. Likewise, U and V are estimated by adding ternary regularization so that the values are $-1,0$, or 1 as much as possible.

## Usage

```
dSVD(X, M=NULL, pseudocount=.Machine$double.eps,
    initU=NULL, initV=NULL, fixU=FALSE, fixV=FALSE,
    Ter_U=1e-10, L1_U=1e-10, L2_U=1e-10, eta=1e+10, J = 3,
    thr = 1e-10, num.iter = 100,
    viz = FALSE, figdir = NULL, verbose = FALSE)
```


## Arguments

X The input matrix which has N-rows and M-columns.
M The mask matrix which has N-rows and M-columns. If the input matrix has missing values, specify the element as 0 (otherwise 1 ).
pseudocount The pseudo count to avoid zero division, when the element is zero (Default: Machine Epsilon).
initU The initial values of factor matrix $U$, which has N-rows and J-columns (Default: NULL).
initV The initial values of factor matrix V, which has M-rows and J-columns (Default: NULL).
fixU Whether the factor matrix $U$ is updated in each iteration step (Default: FALSE).
fixV Whether the factor matrix $V$ is updated in each iteration step (Default: FALSE).
Ter_U Paramter for terary $(-1,0,1)$ regularitation (Default: 1e-10).
L1_U Paramter for L1 regularitation (Default: 1e-10). This also works as small positive constant to prevent division by zero, so should be set as 0 .
L2_U Paramter for L2 regularitation (Default: 1e-10).
eta Stepsize of gradient descent algorithm (Default: 1e+10).
J The number of low-dimension (J $<\{\mathrm{N}, \mathrm{M}\}$, Default: 3)
thr When error change rate is lower than thr, the iteration is terminated (Default: 1E-10).
num.iter The number of interation step (Default: 100).
viz If viz == TRUE, internal reconstructed matrix can be visualized.
figdir The directory for saving the figure, when viz == TRUE.
verbose If verbose $==$ TRUE, Error change rate is generated in console window.

## Value

$\mathrm{U}:$ A matrix which has N -rows and J-columns $(\mathrm{J}<\{\mathrm{N}, \mathrm{M}\})$. V : A matrix which has M-rows and J-columns ( $\mathbf{J}<\{\mathrm{N}, \mathrm{M}\}$ ). RecError : The reconstruction error between data tensor and reconstructed tensor from U and V. TrainRecError : The reconstruction error calculated by training set (observed values specified by M). TestRecError : The reconstruction error calculated by test set (missing values specified by M). RelChange : The relative change of the error.

## Author(s)

Koki Tsuyuzaki

## Examples

```
# Test data
matdata <- toyModel(model = "dSVD")
# Simple usage
out <- dSVD(matdata, J=2, num.iter=2)
```

```
toyModel
```

Toy model data for using $d N M F, d S V D, d s i N M F, d j N M F, d P L S, d N T F$, and dNTD

## Description

The data is used to confirm that the algorithm are properly working.

## Usage

```
toyModel(model = "dNMF", seeds=123)
```


## Arguments

| model | Single character string is specified. "dNMF", "dSVD", "dsiNMF_Easy", "dsiNMF_Hard", |
| :--- | :--- |
| "dPLS_Easy", "dPLS_Hard", "dNTF", and "dNTD" are available (Default: "dNMF"). |  |
| seeds | Random number for setting set.seeds in the function (Default: 123). |

## Value

If model is specified as "dNMF" or "dSVD" a matrix is generated. If model is specified as "dsiNMF_Easy", "dsiNMF_Hard", "dPLS_Easy", or "dPLS_Hard" three matrices are generated. Otherwise, a tensor is generated.

## Author(s)

Koki Tsuyuzaki

## See Also

dNMF,dSVD

## Examples

```
matdata <- toyModel(model = "dNMF", seeds=123)
```


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